



# **Fracture Failure Bodies of Porous Concrete (foam = similar behavior), Normal Concrete, Ultra-High-Performance-Concrete and of the Lamella Sheet**

***- generated on basis of Cuntze's Failure-Mode-Concept (FMC)***

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Presentation captures all models of the fracture bodies 'concrete' engineering' needs

1. **Motivation for a novel Concept to generate Strength Criteria**
2. **Basic Ideas of Cuntze's Failure-Mode-Concept (FMC)**
3. **Application to porous Concrete Stones (Ytong, Hebel)** (*similar to foam material*)
4. **Application to Normal Concrete**
5. **Application to UHPC (Ultra High Performance Concrete)**
6. **Application to transversaly-isotropic CFRP-Sheets (Polymer-Matrix Lamina)**

*2D test data available, just of a similar behaving material*

*3D test data available*

*3D test data available*

*own 2D test data and further 3D were available*

- *A similar behaving material gives the possibility to set up the Shape of a model*
- *Measured strength data of the novel material fix the Size of the obtained model*

*for armouring in construction rehabilitation  $\equiv$  CFRP in concrete*

**Results of a time-consuming, never funded "hobby" of a retired engineer**



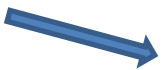
## CONSTRAINTS in Design Development Process : *Cost and Time Reduction*

Industry looks for **robust & reliable analysis procedures** in order to replace the expensive ‘Make and Test Method’ as far as reasonable.

Some *testing* remains mandatory in order to figure out *together with the modeling* sufficient knowledge about the behavior of materials and structural parts.

**Dependent on the gained knowledge**  
**Virtual Tests will *reduce the amount of* Physical Tests.**

Thereby an *improved modeling*  
will support





## Therein one instrument is the application of Validated **Strength Failure Conditions SFCs** (strength criteria)

These analysis tools involve SFCs for the failure types:

Yielding (ductile inelastic behaving materials),

Fracture (**brittle** behaving materials) which means

**fracture strength failure conditions**  $F(\sigma, R) = 1$  for **obtaining Design Verification.**

in civil engineering:  
strength  $R = f$

$F$  = failure function,  $\sigma$  = stress,  $R = f$  (in civil engineering) = strength  
4



# The Strength Fracture Body

The surface of the so-called **fracture body** is

- mathematically described by  **$F$**

- built up by the tips of

all multi-axial stress vectors which 'almost' lead to fracture.

For all these fracture stress states is valid:

the **reserve factor**  $RF = 1$ , or its inverse

the so-called **material stressing effort**  $Eff = 1 = 100\%$  (Werkstoffanstrengung)

$$= 1 / RF$$

$F$  = failure function,  $\sigma$  = stress,  $R = f$  (in civil engineering) =  $\frac{\text{strength}}{5}$



# What was the driving idea behind when generating the FMC ?

To search a possibility

for brittle behaving materials

to *more generally* formulate - for fracture failure -  
appropriate strength failure conditions (SFCs) :

- failure mode-wise (*shear yielding failure, etc.*)

- stress invariant-based ( $J_2$  etc.)

- obtaining equivalent stresses .

*analogously to :*

**Mises, Hashin, Puck etc.**

**Mises, Tsai, Hashin, Christensen,  
etc.**

**Mises for shear yielding,  
Rankine for fracture**

$$e.g. \text{ 'Mises': } 6 \cdot J_2 = (\sigma_I - \sigma_{II})^2 + (\sigma_{II} - \sigma_{III})^2 + (\sigma_{III} - \sigma_I)^2 = f(\tau)$$



# So-called Global and Modal Strength Failure Conditions (SFCs): Description

- **Global SFC (lumped):** *Prager, Ottosen, Willam-Warnke, Tsai*  
describes the full failure surface by one single equation capturing all existing failure modes such as Normal fracture NF or Shear Fracture SF
- **Modal SFC :** *Cuntze , Mises for the mode yielding,*  
describes each failure mode-associated part of the full failure surface by a single equation.

**more detailed**  
→



# Global versus Modal Strength Failure Conditions (criteria)

**1 Global strength failure condition** :  $F(\{\sigma\}, \{R\}) = 1$  (usual formulation)

**Set of Modal strength failure conditions**:  $F(\{\sigma\}, R^{mode}) = 1$  (addressed in FMC)

*Example: UD*

vector of 6 stresses (general)

vector of 5 strengths

$$\{\sigma\} = (\sigma_1, \sigma_2, \sigma_3, \tau_{23}, \tau_{31}, \tau_{21})^T \quad \{R\} = (R_{||}^t, R_{||}^c, R_{\perp}^t, R_{\perp}^c, R_{\perp||})^T$$

needs an **Interaction of Failure Modes**: performed here by a  
*probabilistic-based 'rounding-off' approach (series failure system model)*  
*directly delivering the (material) reserve factor in linear analysis*

in civil engineering:  
strength  $R = f$

**A modal concept** – as found with Cuntze (general) and Puck (for UD material) , Mises (isotropic) –  
**builds up the Fracture Failure Surface mode-wise !**





Helpful for the designing engineer is the delivery of **equivalent stresses** and of the **material stressing effort** *Eff*.

*mode* **material stressing effort** \* (in German “Werkstoffanstrengung”)

The relationship is

$$Eff^{mode} = \sigma_{eq}^{mode} / R^{mode}$$

*mode* **equivalent stress**

*mode* **associated average strength** (bar over)

*anology to ‘Mises’*

$$Eff^{fracture\ mode} = \sigma_{eq}^{fracture\ mode} / R_m$$

$$Eff^{Mises} = \sigma_{eq}^{Mises} / R_{po.2}$$

\* **material stressing effort** *Eff* = *artificial technical term* , created together with *QinetiQ, UK*, during the *Wotrld-Wide-Failure-Exercises*



**Interaction** of adjacent Failure Modes by a '*series failure system*' model in the mode transition zones

= 'Accumulation' of interacting *failure danger portions*  $Eff^{mode}$

$$Eff = \sqrt[m]{(Eff^{mode\ 1})^m + (Eff^{mode\ 2})^m + \dots} = 1 = 100\%, \text{ if failure}$$

with mode-interaction exponent  $m$ , from mapping experience

It is assumed engineering-like :  $m$  takes the same value for all mode transition zones captured by the interaction formula above



# Basic Ideas of Cuntze's FMC

- Use of invariants (see Mises), which are linked to a physical mechanism of the deforming solid:  
Following Beltrami, Mises and Mohr-Coulomb: *for isotropic materials*
  - volume change :  $\mathbf{I}_1^2$  ... (*dilatational energy*)
  - shape change :  $\mathbf{J}_2$  (v. Mises) . (*distortional energy*)
  - friction :  $\mathbf{I}_1$  ... (*friction energy*)
- A closed Ansatz-function  $F = 1$  for the fracture body (or a part of it), despite of a possible non-circularity of the meridians
- All parameters are measurable: strengths  $R$  and material friction  $\mu$

*isotropic invariants : concrete*

$$I_1 = (\sigma_I + \sigma_{II} + \sigma_{III})^T = f(\sigma) , \quad 6J_2 = (\sigma_I - \sigma_{II})^2 + (\sigma_{II} - \sigma_{III})^2 + (\sigma_{III} - \sigma_I)^2 = f(\tau)$$

$$27J_3 = (2\sigma_I - \sigma_{II} - \sigma_{III}) \cdot (2\sigma_{II} - \sigma_I - \sigma_{III}) \cdot (2\sigma_{III} - \sigma_I - \sigma_{II})$$

*anisotropic invariants : transversely-isotropic UD-sheet*

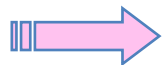
$$I_1 = \sigma_1, \quad I_2 = \sigma_2 + \sigma_3, \quad I_3 = \tau_{31}^2 + \tau_{21}^2, \quad I_4 = (\sigma_2 - \sigma_3)^2 + 4\tau_{23}^2, \quad I_5 = (\sigma_2 - \sigma_3)(\tau_{31}^2 - \tau_{21}^2) - 4\tau_{23}\tau_{31}\tau_{21}$$



- 1 If a material element can be homogenized to an ideal (= frictionless) crystal, then, **material symmetry** demands for the transversely-isotropic UD-material
  - 5 elastic 'constants'  $E, \nu$ ; 5 strengths  $R$ ; 5 fracture toughnesses  $K_c$  and
  - 2 physical parameters (such as CTE, CME, material friction value  $\mu$  etc.)

*(for isotropic materials the respective numbers are 2 and 1)*
- 2 **Mohr-Coulomb** requires for the real crystal another inherent parameter,
  - the physical parameter '**material friction**': UD  $\mu_{\perp\parallel}, \mu_{\perp\perp}$ ; isotropic  $\mu$
- 3 **Fracture morphology Observations** witness:
  - Each strength corresponds to a distinct *failure mode*

and to a *fracture type* as Normal Fracture (NF) or Shear Fracture (SF).



above Facts and Knowledge gave the reason  
why the FMC strictly employs single independent failure modes  
in its failure mode-wise concept.



## Detailed Fracture Morphology Impacts on the Failure-Mode-Concept (FMC)

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- Each failure mode represents 1 independent failure mechanism  
and thereby 1 piece of the complete *failure surface*
- Each failure mechanism is governed by 1 basic strength (is observed !)
- Each failure *mode* can be represented by 1 failure *condition*.

Therefore, *equivalent stresses* can be computed for each *mode* !



# Cuntze's 3D-Strength Failure Conditions (criteria) for Isotropic Foams, concrete stone

1. SFCs:

$$F^{NF} = \frac{\sqrt{4J_2 - I_1^2/3} + I_1}{2 \cdot \bar{R}_t} = 1$$

Normal Fracture  
NF, tension

$$F^{CrF} = \frac{\sqrt{4J_2 - I_1^2/3} - I_1}{2 \cdot \bar{R}_c} = 1$$

Crushing Fracture  
CrF, compressive  
meridian

Ductile behaviour: one failure mechanism or mode, Mises Yielding. Brittle behaving foam: 2 failure modes NF and CrF.

2. Considering tensile meridian (bi-axial strength points, failure mode occurs twofold, causing dents on meridians):

Two-fold failure danger can be excellently modelled by employing the often used invariant  $J_3$

$$\Theta_{NF} = \sqrt[3]{1 + D_{NF} \cdot \sin(3\theta)} = \sqrt[3]{1 + D_{NF} \cdot 1.5 \cdot \sqrt{3} \cdot J_3 \cdot J_2^{-1.5}} \quad \Theta_{CrF} = \sqrt[3]{1 + D_{CrF} \cdot \sin(3\theta)} = \sqrt[3]{1 + D_{CrF} \cdot 1.5 \cdot \sqrt{3} \cdot J_3 \cdot J_2^{-1.5}}$$

$$Eff^{NF} = c_{NF} \cdot \frac{\sqrt{4J_2 \cdot (\Theta_{NF}) - I_1^2/3} + I_1}{2 \cdot \bar{R}_t} = \frac{\sigma_{eq}^{NF}}{\bar{R}_t} \quad \text{in Effs now} \quad Eff^{CrF} = c_{CrF} \cdot \frac{\sqrt{4J_2 \cdot (\Theta_{CrF}) - I_1^2/3} - I_1}{2 \cdot \bar{R}_c}$$

3. Mode interaction:  $Eff^m = (Eff^{NF})^m + (Eff^{CrF})^m = 1$  = surface description of fracture body

4. Closures at both the ends: A paraboloid serves as closing cap and bottom

$$\frac{I_1}{\sqrt{3} \cdot \bar{R}_t} = s_{cap} \cdot \left( \frac{\sqrt{2J_2 \cdot \Theta_{NF}}}{\bar{R}_t} \right)^2 + \frac{\max I_1}{\sqrt{3} \cdot \bar{R}_t} \quad \text{auf die } R_t\text{-normierten} \\ \text{Lodekoordinaten bezogen} \quad \frac{I_1}{\sqrt{3} \cdot \bar{R}_t} = s_{bot} \cdot \left( \frac{\sqrt{2J_2 \cdot \Theta_{CrF}}}{\bar{R}_t} \right)^2 + \frac{\min I_1}{\sqrt{3} \cdot \bar{R}_t}$$

The slope parameters  $s$  are determined connecting the respective hydrostatic strength point with the associated point on the tensile and on the compressive meridian,  $maxI_1$  must be assessed whereas  $minI_1$  can be measured.  $D$  = non-circularity parameter

meridian:= axial cut of fracture body

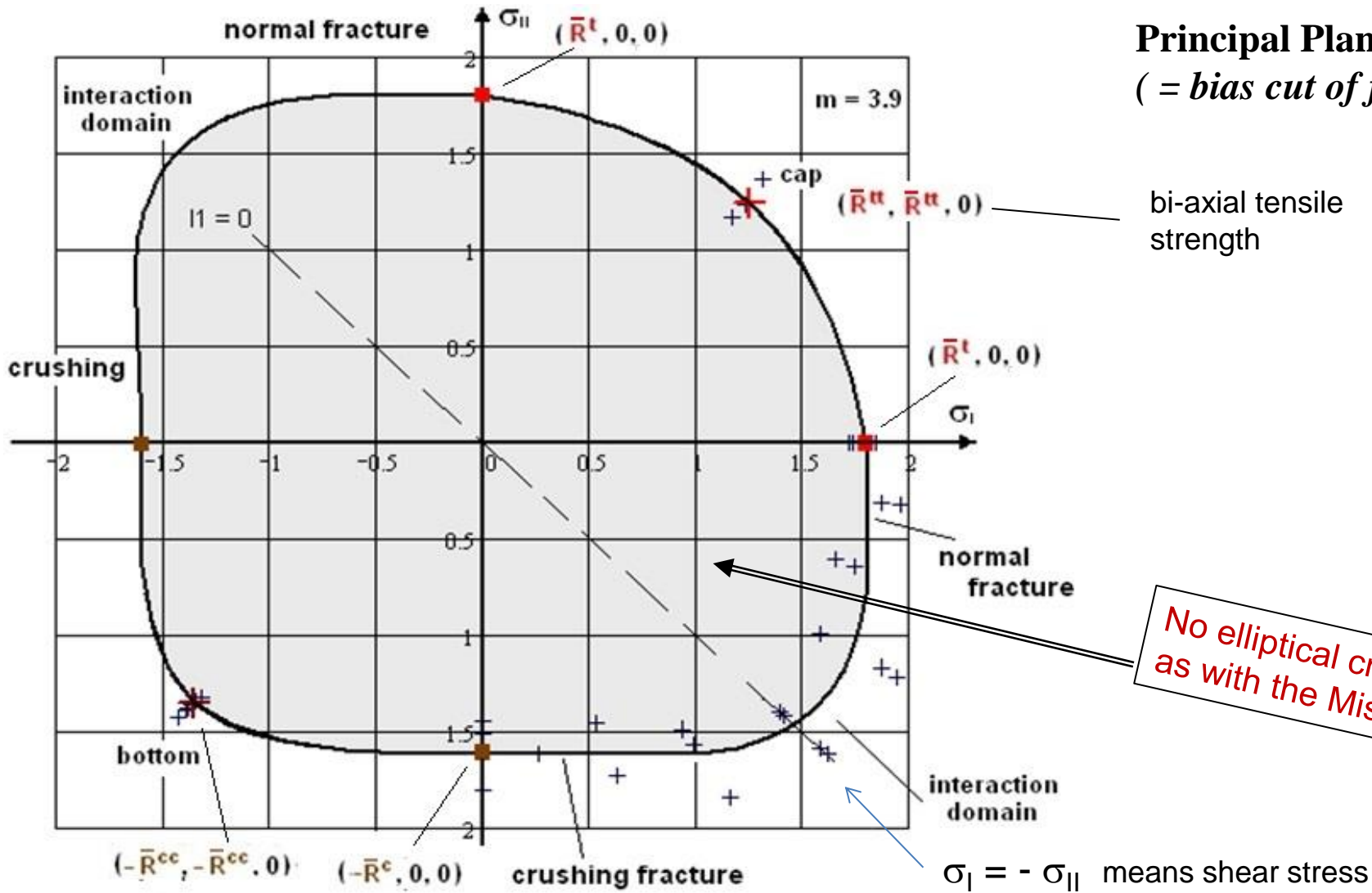


Is the multi-axially tested fracture body (model) known  
from a similarly behaving material, then

- the Shape of the fracture body of the new material is known and only
- the Size must be fixed by the always to be provided (uni-axial) strengths .

*Example fracture body : foam, known >> concrete stone, thereby predictable*

# 2D - Test Data Set and Mapping in the Principal Stress Plane (*brittle, porous*)



Principal Plane Cross-section  
(= bias cut of fracture body)  $\sigma_{II}(\sigma_I)$

Concrete Stone:  
Similar behaviour to  
*Rohacell 71 IG*

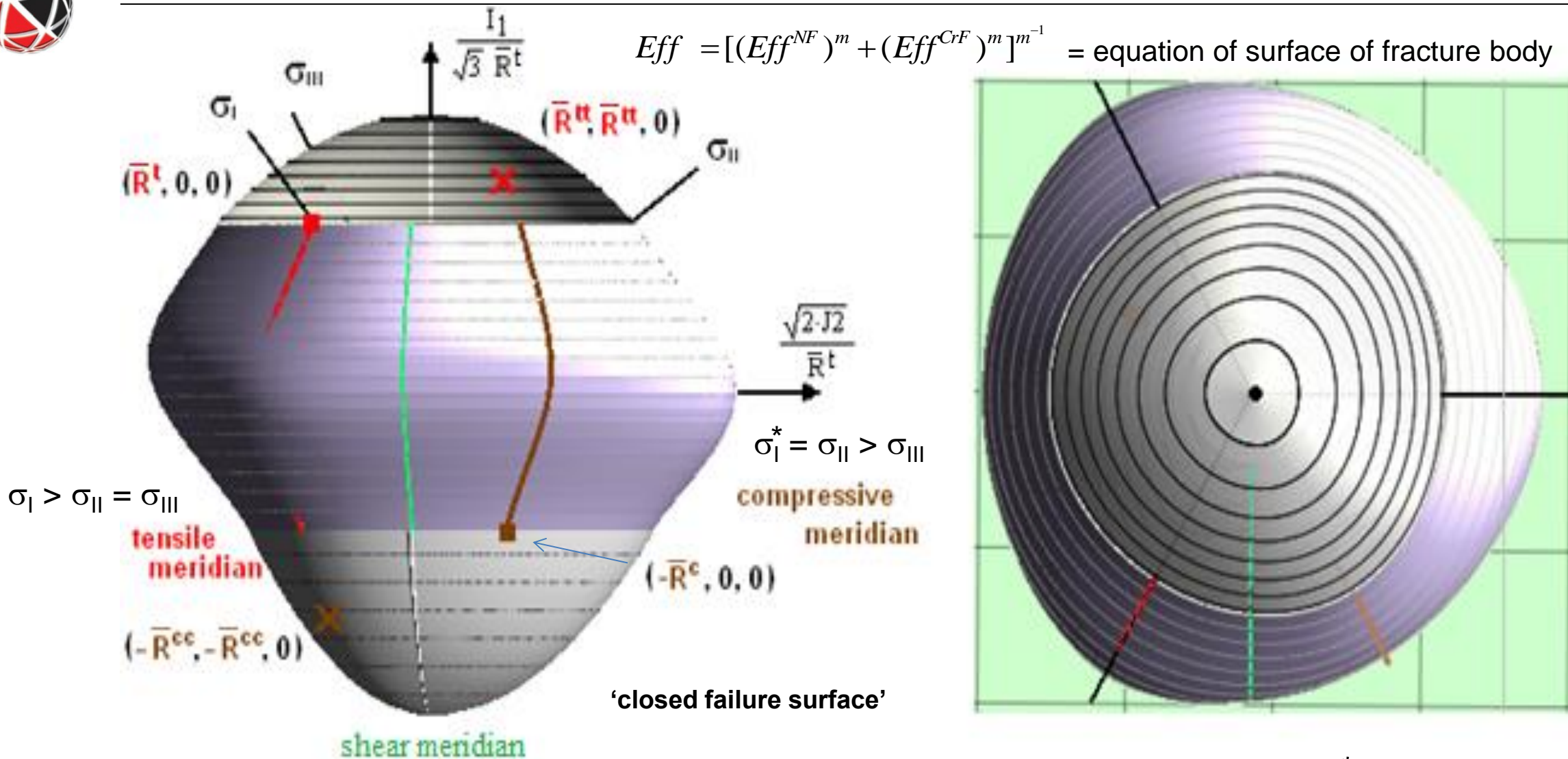
No elliptical cross-section  
as with the Mises-cylinder!

- Mapping must be performed in the 2D-plane because fracture data set is given there
- The 2D-mapping uses the 2D-subsolution of the 3D-strength failure conditions
- The 3D-fracture failure surface (body) is based on the 2D-derived model parameters.





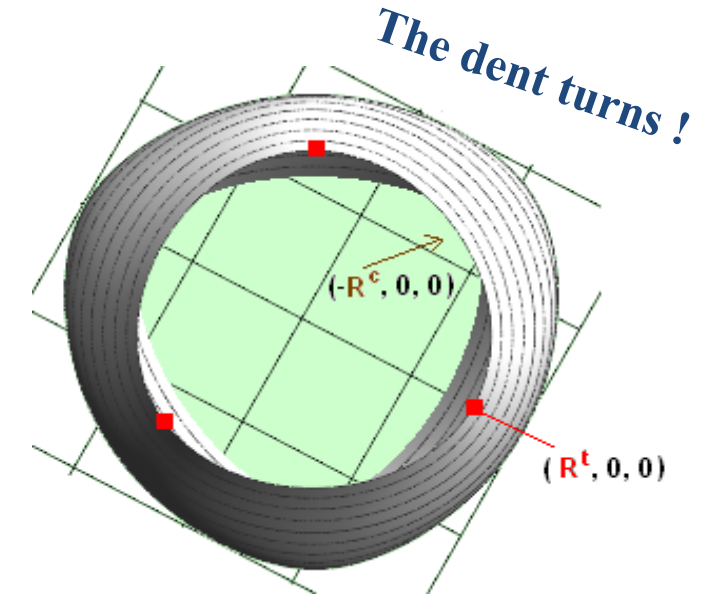
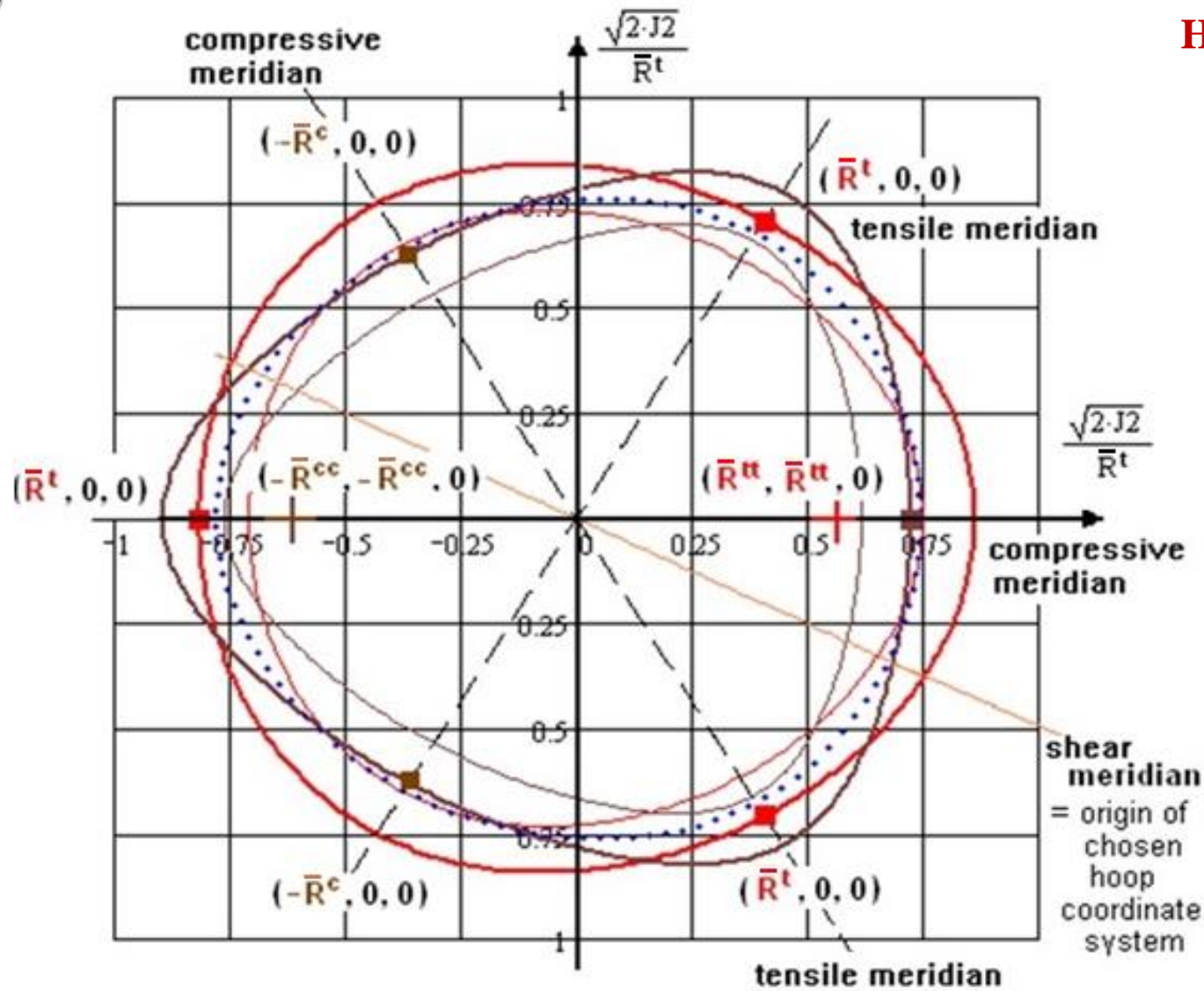
# Fracture Failure Surface (body) and main Meridians of *Rohacell 71 IG foam (similar to concrete stone)*



Fracture body of a porous concrete stone with its different meridians (left) and view from top (right).  $R := strength \equiv f$ ,  $t := tensile$ ,  $c := compressive$ . bar over means mean value,  $J_2 :=$  'Mises' - invariant,  $I_1 :=$  sum of principal stresses. (Mathcad plot. Test data, courtesy V. Kolupaev, LBF).  $s_{cap} = -0.56$ ,  $s_{bot} = 1.09$ ,  $d_{NF} = 0.17$ ,  $d_{CrF} = -0.55$ ,  $c_{NF\theta} = 0.98$ ,  $c_{CrF\theta} = 0.95$

\* here:  $\sigma_I$  is the mathematically largest stress (most positive one) or Mohr stress

Hoop Cross-sections of the Fracture Body at various  $I_1$  - levels



Caps: No test data, cone chosen

at  $I_1 = 0$  a circle.

with characteristic uni-axial and bi-axial strength points X



# Cuntze's 3D- SFCs for Concrete

Concrete:

$$F^{NF} = c_{NF} \frac{\sqrt{4J_2 \cdot \Theta_{NF} - I_1^2 / 3 + I_1}}{2 \cdot \bar{R}^t} = 1$$

$$F^{SF} = c_{1SF} \cdot \frac{3J_2 \cdot \Theta_\tau}{\bar{R}^c} + c_{2SF} \cdot \frac{I_1}{\bar{R}^c} = 1$$

or in *Eff*s after insertation  $\sigma = \text{Eff} \cdot R$  into the invariants within  $F = 1$

$$\text{Eff}^{NF} = c_{NF} \cdot \frac{\sqrt{4J_2 \cdot \Theta_{NF} - I_1^2 / 3 + I_1}}{2 \cdot \bar{R}^t} = \sigma_{eq}^{NF} / \bar{R}^t, \quad \text{Eff}^{SF} = \frac{c_{2SF} \cdot I_1 + \sqrt{(c_{2SF} \cdot I_1)^2 + 12 \cdot c_{1SF} \cdot 3J_2 \cdot \Theta_{SF}}}{2 \cdot \bar{R}^c} = \sigma_{eq}^{SF} / \bar{R}^c,$$

$D$  = non-circularity parameter.  $I_1$  considers friction

$$\Theta = \sqrt[3]{1 + D \cdot \sin(3\theta)} = \sqrt[3]{1 + D \cdot 1.5 \cdot \sqrt{3} \cdot J_3 \cdot J_2^{-1.5}}$$

consideration of volume change (vc) under high hydrostatic pressure (if required)

considering Volume change:

$$F^{NF} = c_{NF} \frac{\sqrt{4J_2 \cdot \Theta_{NF} - I_1^2 / 3 + I_1}}{2 \cdot \bar{R}^t} = 1$$

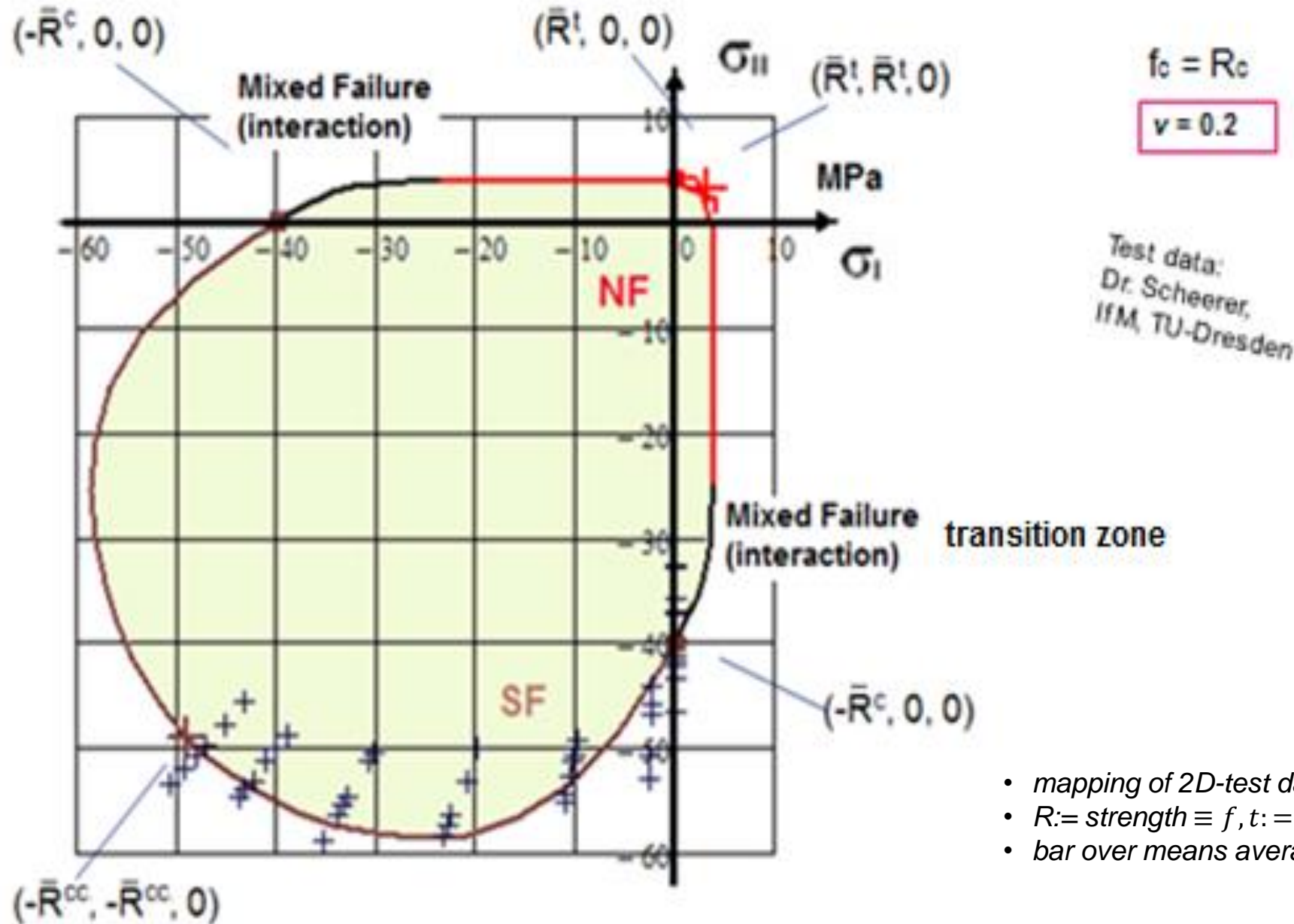
$$F^{SFvc} = c_{1vc} \cdot \frac{3J_2 \cdot \Theta_\tau}{\bar{R}^c} + c_{2vc} \cdot \frac{I_1}{\bar{R}^c} + c_{3vc} \cdot \frac{I_1^2}{\bar{R}^c} = 1$$

For higher Poisson ratios it must be checked for higher Poisson ratios  $\mu$ , whether under high bi-axial compression ( $\sigma_x, \sigma_y, \sigma_{ax} = 0$ ) the axial strain approaches the tensile fracture strain !.

**Lesson Learned:** A physics-based SFC – usually – describes just one single failure mechanism or mode and does not capture the bi-axial effect of  $\sigma_I = \sigma_{II}$ , which means capturing a two-fold acting mode



# Normal Concrete: Principal Stress Plane = bias cut of fracture body $\sigma_{II}(\sigma_I)$



- mapping of 2D-test data in the principal stress plane.
- $R$ := strength  $\equiv f$ ,  $t$ : = tensile,  $c$ : = compressive;
- bar over means average value





# Normal Concrete: Fracture Body with its differently deformed meridians

compressive strength point

tensile meridian

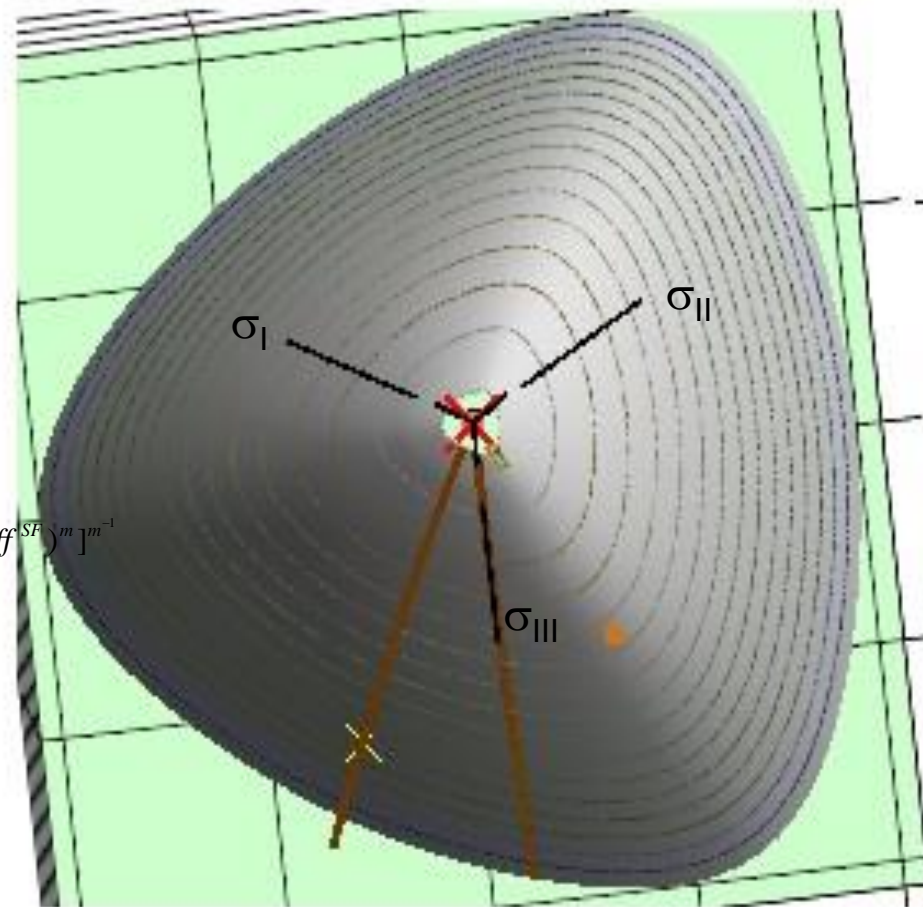
compressive meridian

shear meridian

'open failure surface'

biaxial compressive strength point

$$Eff = [(Eff^{NF})^m + (Eff^{SF})^m]^{m^{-1}}$$



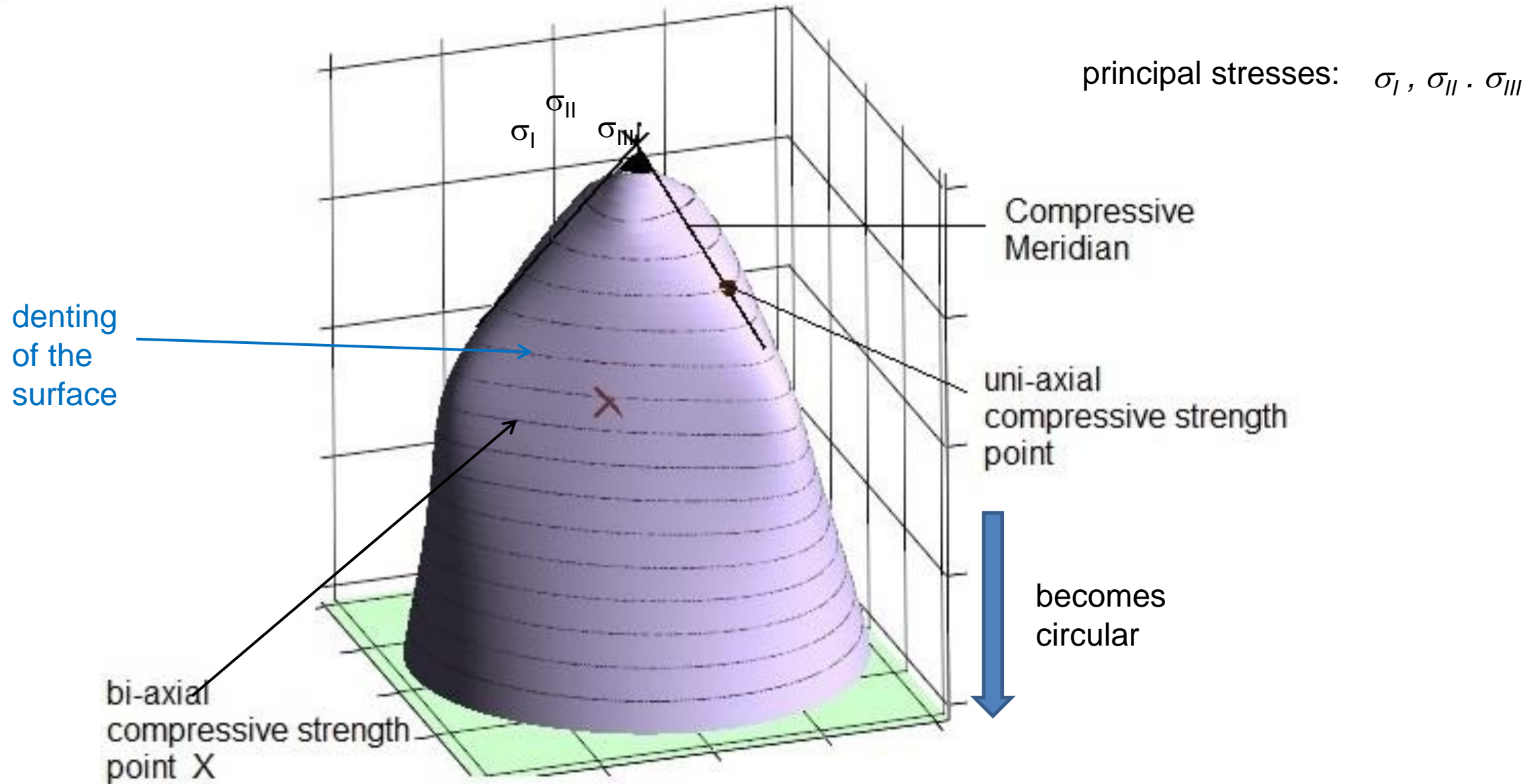
$$Eff = [(Eff^{NF})^m + (Eff^{SF})^m]^{m^{-1}} = 1 \quad \text{is equation of surface of fracture body}$$

$max I_1 = 8.4 \text{ MPa}$  (Mathcad plot)

*The non-coaxiality decreases with hydrostatic pressure, cross-section becomes circular!*



# Ultra-High-Performance-Concrete (UHPC): Fracture Body



# Cuntze's 3D-SFCs for UD-materials (sheet, lamella) *several times presented at NAFEMS*

(top-ranked in the World-Wide-Failure-Exercises-I and -II, 1991-2013. Cuntze is like a simple 'Mises' amongst the UD-SFCs

FF1  $Eff^{||\sigma} = \bar{\sigma}_1 / \bar{R}_{||}^t = \sigma_{eq}^{||\sigma} / \bar{R}_{||}^t,$

$\bar{\sigma}_1^* \cong \varepsilon_1^t \cdot E_{||}$  filament strains from FEA captures axial tensile straining under bi-axial compression

FF2  $Eff^{||\tau} = -\bar{\sigma}_1 / \bar{R}_{||}^c = +\sigma_{eq}^{||\tau} / \bar{R}_{||}^c,$

$\bar{\sigma}_1 \cong \varepsilon_1^c \cdot E_{||}$  2 filament modes

IFF1  $Eff^{\perp\sigma} = [(\sigma_2 + \sigma_3) + \sqrt{(\sigma_2 - \sigma_3)^2 + 4\tau_{23}^2}] / 2\bar{R}_{\perp}^t = \sigma_{eq}^{\perp\sigma} / \bar{R}_{\perp}^t$

IFF2  $Eff^{\perp\tau} = [(\frac{\mu_{\perp\perp}}{1 - \mu_{\perp\perp}}) \cdot (\sigma_2 + \sigma_3) + \frac{1}{1 - \mu_{\perp\perp}} \sqrt{(\sigma_2 - \sigma_3)^2 + 4\tau_{23}^2}] / \bar{R}_{\perp}^c = +\sigma_{eq}^{\perp\tau} / \bar{R}_{\perp}^c$

3 'matrix' modes

IFF3  $Eff^{\perp||} = \{ [2\mu_{\perp||} \cdot I_{23-5} + (\sqrt{(2\mu_{\perp||})^2 \cdot I_{23-5}^2 + 4 \cdot \bar{R}_{\perp||}^2 \cdot (\tau_{31}^2 + \tau_{21}^2)})^2] / (2 \cdot \bar{R}_{\perp||}^3) \}^{0.5} = \sigma_{eq}^{\perp||} / \bar{R}_{\perp||}$

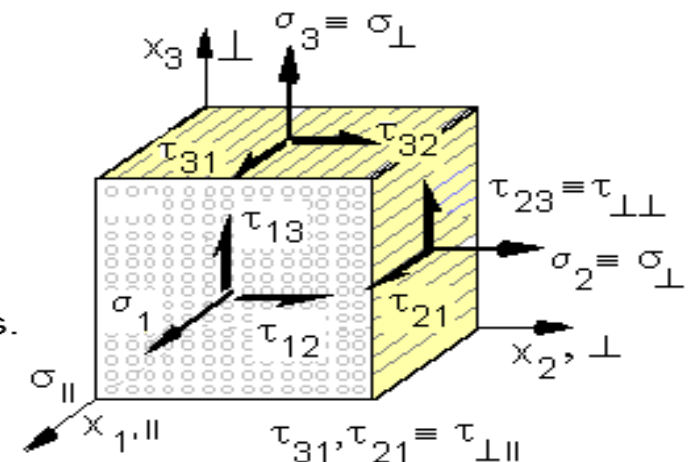
with  $I_{23-5} = 2\sigma_2 \cdot \tau_{21}^2 + 2\sigma_3 \cdot \tau_{31}^2 + 4\tau_{23}\tau_{31}\tau_{21}$  [Cun04, Cun11]

Modes-Interaction  $Eff^m = (Eff^{||\tau})^m + (Eff^{||\sigma})^m + (Eff^{\perp\sigma})^m + (Eff^{\perp\tau})^m + (Eff^{\perp||})^m$

with influence IFF on FF: = 1 = 100% is 'onset of failure'

with mode-interaction exponent  $2.5 < m < 3$  from mapping test data

Typical friction value data range:  $0.05 < \mu_{\perp||} < 0.3, 0.05 < \mu_{\perp\perp} < 0.2$



Eff:= material stressing effort (Werkstoffanstrengung), R:= UD strength,  $\sigma_{eq}$ := equivalent stress.  
 Eff:= artificial word, fixed with QinetiQ in 2011, to have an equivalent English term.  
 Poisson effect considered\*: bi-axial compression strains a filament without any  $\sigma_1$   
 t:= tensile, c:= compression, || := parallel to fibre,  $\perp$  := transversal to fibre

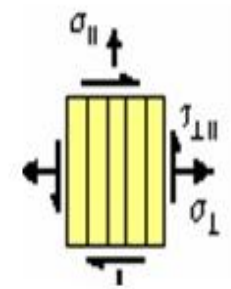
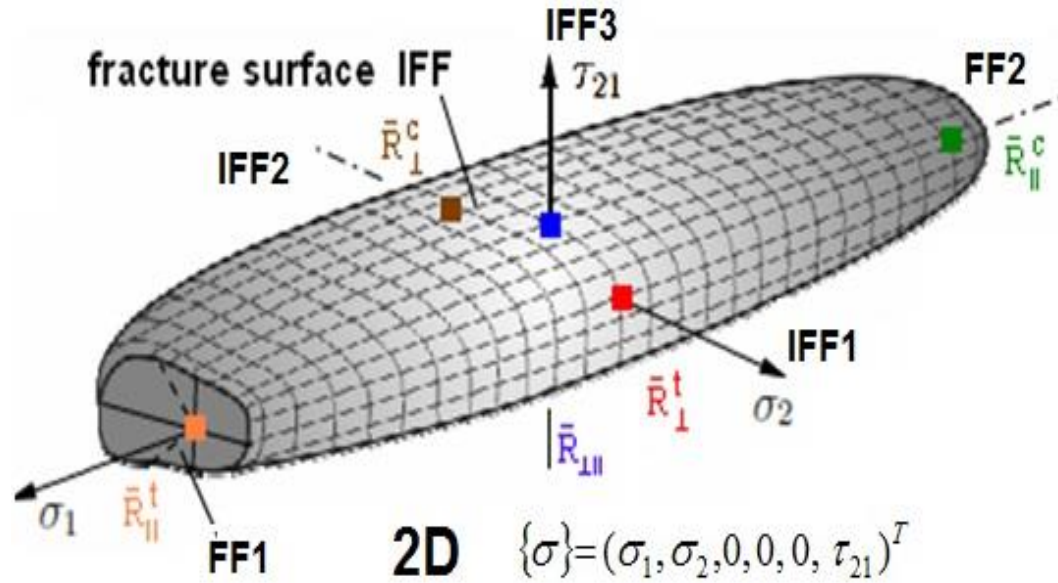




# UD Fracture Body for isolated Lamina, Sheet (lamella)

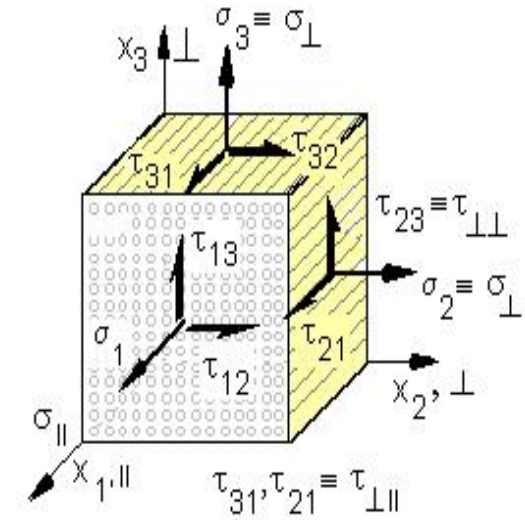
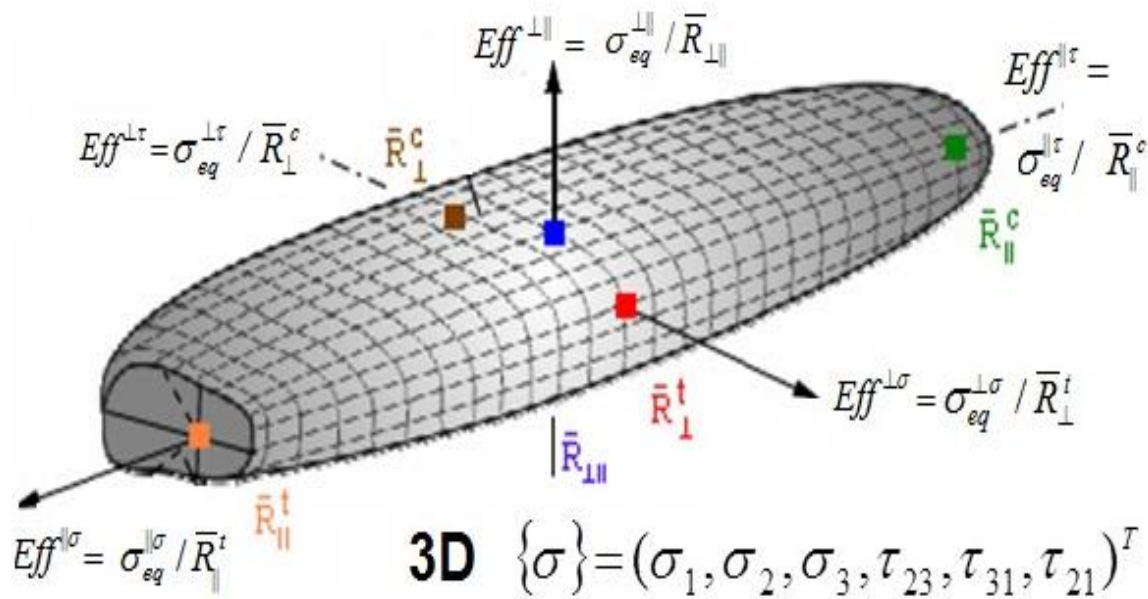
UD = uni-directional

2 D:  
 $\sigma$



2D >> 3D  
after replacing  
 $\sigma, \tau$  by  $\sigma_{eq}^{mode}$

3 D:  
 $\sigma_{eq}$



$\nu_{\perp\perp} = 0.4,$   
 $\nu_{\perp\parallel} = 0.3$





## Conclusions

- **The FMC is a general applicable efficient concept, which**  
is applicable to brittle and ductile, dense and porous, isotropic, transversely-isotropic and orthotropic materials  
improves prediction + simplifies design verification and **delivers equivalent stresses**
- **uses just the measurable model parameters strength  $R$  and material friction  $\mu$**
- **builds** not on the **material type** but on the ***deformation behaviour + texture of the material***
- **delivers a combined formulation of *independent failure modes*,**  
**without the well-known drawbacks of a global formulation**  
(= '*mathematically forced marriage*' of *in-dependent failure modes*)
- **FMC-based Strength Failure Conditions are relatively simple but describe physics of each single failure mechanism pretty well.**
- **Mapping of above brittle behaving materials was successful; lead to some new findings !**



**„The generation of reliable multi-axial fracture test data  
with the understanding of the associated fracture mechanisms  
is a more effortful work  
than the establishment of a theory.**

**However mind,  
a reliable theory, only,  
makes the whole practicable.“**

*Experience from Ralf Cuntze*



## Some Literature

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## For mutual understanding: *What do the following terms mean ??*

**Material** : homogenized (macro-)model of the envisaged solid

**Failure** : structural part does not fulfil a distinct functional requirement

such as onset of yielding, onset of brittle fracture, leakage, delamination size limit,  
frequency bound .

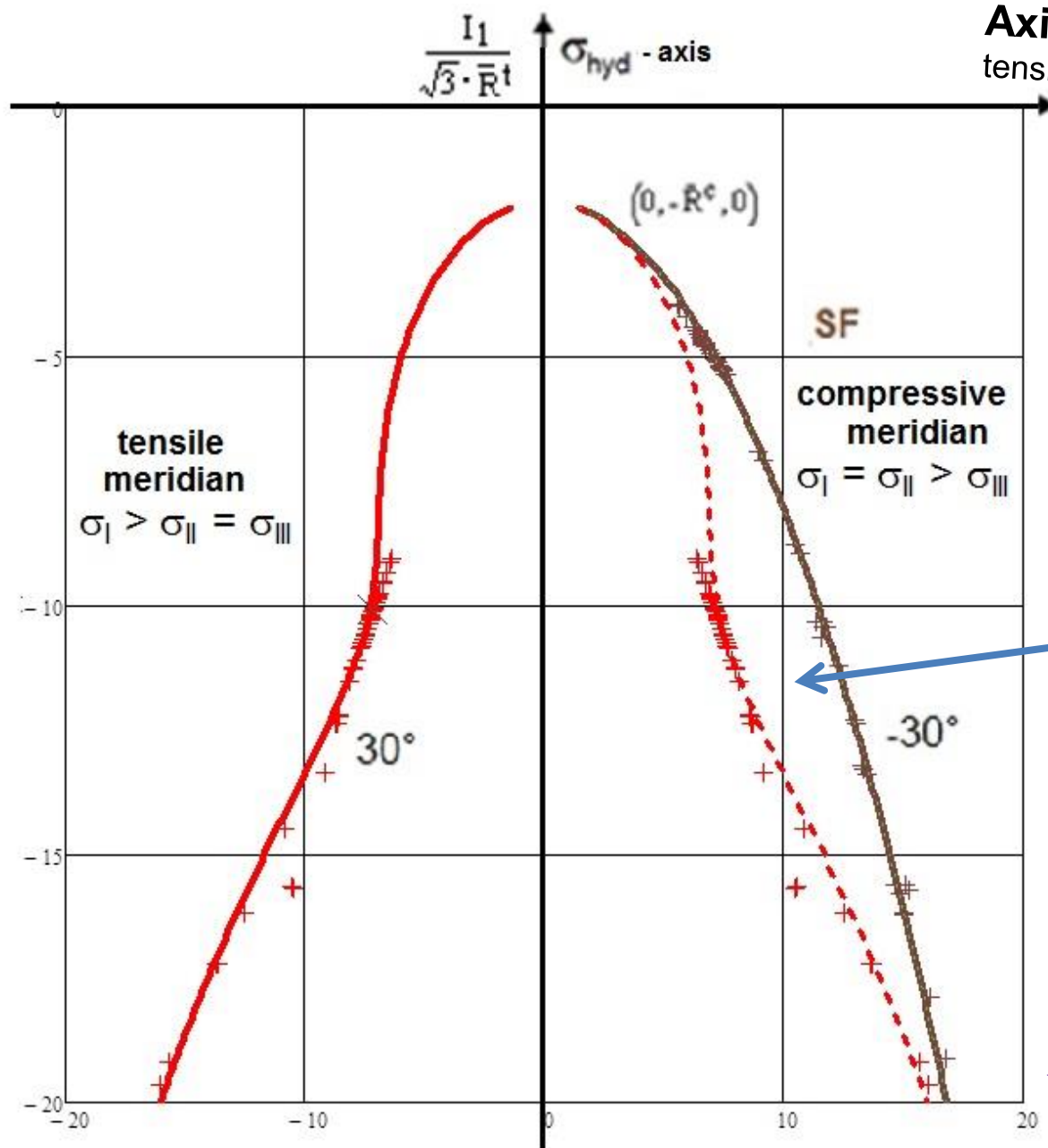
**Strength Failure Condition (SFC):**

Condition to assess a 'multi-axial failure stress state ' in a critical location of the structural part  
= mathematical formulation of the failure surface of the fracture body :  $F = 1$

(which is now falsely termed strength criterion , that is defined as  $F \geq < 1$ ).



# Ultra-High-Performance-Concrete: Tensile and Compressive Meridian



## Axial cross-section of the fracture body

tensile meridian and compressive meridian are opposite to another

### Procedure with respect to MATHCAD capabilities and with consideration of the confined non-circularity

(both the curves come together) :

- Fitting of the course of compressive test data using linear progression in MATHCAD
- Estimation of non-circularity parameter  $D$
- Prediction of tensile meridian curve

$$\bar{R}^t = 20 \text{ MPa}, \bar{R}^c = 160 \text{ MPa}, \bar{R}'' = 0.89 \cdot \bar{R}^t \text{ (assumed)},$$

$$\bar{R}^{cc} = 175 \text{ MPa}$$

**Mohr stresses:**  $\sigma_I, \sigma_{II}, \sigma_{III}$

end of non-circularity,

MATHCAD : Indirect fitting with Linear Progression tool which allows just a mapping of the compression meridian and a further step to consider the different denting between the compression and the tensile meridian plus to consider the end of the non-coaxiality.

*(Original test data, courtesy K. Speck, IfM Dresden. Evaluated by the author for the tensile and compressive meridians.)*

The direct fitting tool MINIFIT did not work unfortunately in contrast to the previous experience